

Worksheet 3 Binary arithmetic

Data types



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Worksheet 3 Binary arithmetic **Answers**

Task 1

Carry out the following binary sums showing your working out:

a) $101_2 + 111_2$

| | | | | | |
|---|---|---|---|--|--|
| | | 1 | 1 | | |
| | 1 | 0 | 1 | | |
| | 1 | 1 | 1 | | |
| 1 | 1 | 0 | 0 | | |

b) $10110_2 + 10111_2$

| | | | | | | |
|---|---|---|---|---|---|---|
| 1 | | | 1 | 1 | | |
| | 1 | 0 | 1 | 1 | 1 | 0 |
| | 1 | 0 | 1 | 1 | 1 | 1 |
| 1 | 0 | 1 | 1 | 0 | 0 | 1 |

c) $11_2 + 100001_2 + 101_2$

| | | | | | | | |
|---|---|---|---|---|---|---|--|
| | | | 1 | 1 | 1 | | |
| | | | | | 1 | 1 | |
| 1 | 0 | 0 | 0 | 0 | 0 | 1 | |
| | | | | 1 | 0 | 1 | |

d) $10101_2 + 111011_2 + 1001_2$

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 1 | 1 | 1 | 1 | 1 | | |
| | | | 1 | 0 | 1 | 0 | 1 |
| | | 1 | 1 | 1 | 0 | 1 | 1 |
| | | | | 1 | 0 | 0 | 1 |

Show how the following values can be stored as binary bytes within a computer system and determine the answer that would be calculated and stored:

e) $12_{10} + 13_{10}$

| 12 | 64 | 32 | 16 | 8 | 4 | 2 | 1 |
|----|----|----|----|---|---|---|---|
| 8 | | | | | | | |
| 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |

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f) $174_{10} + 255_{10}$

| | | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|
| | | | | | | | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | | | |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 1 | |

g) $19_{10} + 66_{10} + 74_{10}$

| | | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|
| 1 | | | | | | 1 | | | | | | | | | | | |
| 0 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | |
| 0 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 | |
| 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |

Answer the following question:

h) A computer has been designed to work only in single bytes of data. Describe the problem that will be encountered when carrying out the sum $01111001_2 + 11111001_2$ if the answer is only allocated one byte of storage.

- The answer is 101110010 which is 9 bits
- A byte is 8 bits so answer is too long to store and byte would be 01110010
- Calculation results in an overflow error indicating the resulting 8 bits have an incorrect answer and should be discarded

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Task 2 Binary subtraction **Answers**

Convert these decimal values into two's complement binary bytes:

a) $-50_{10} = 11001110$

b) $-120_{10} = 10001000$

c) $127_{10} = 01111111$

d) $-128_{10} = 10000000$

e) Show that -50_{10} gives the same result as in (a) above using the following alternative method:

Assume the left-most bit represents -128. Start at -128 and then add the remaining values:

| - | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 |
|---|----------|----------|----------|----------|----------|----------|----------|----------|
| | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 |

Carry out the following calculations in two's complement binary bytes:

f) $-50_{10} - 30_{10}$ or $-50_{10} + -30_{10}$

| | | | | | | | |
|----------|----------|----------|----------|----------|----------|----------|----------|
| 1 | | | 1 | 1 | 1 | | |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |

g) $-66_{10} + 34_{10}$

| | | | | | | | |
|----------|----------|----------|----------|----------|----------|----------|----------|
| | 1 | 1 | 1 | 1 | 1 | | |
| 1 | 0 | 1 | 1 | 1 | 1 | 1 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 1 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |

h) $-88_{10} - 12_{10}$

| | | | | | | | |
|----------|----------|----------|----------|----------|----------|----------|----------|
| 1 | 1 | | | | | | |
| 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 |

i) $22_{10} - -14_{10}$

| | | | | | | | |
|----------|----------|----------|----------|----------|----------|----------|----------|
| | | 1 | 1 | 1 | 1 | | |
| 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 |
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 |
| 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 |

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Task 3 Fixed point binary Answers

Convert these decimal values into a fixed-point binary byte where the first 4 bits represent the whole number part and the the last 4 bits represent the fractional part:

- a) 8.5_{10} = 10001000
- b) 14.25_{10} = 1110 0100
- c) 0.125_{10} = 00000010
- d) 5.5625_{10} = 01011001
- e) 1.9375_{10} = 00011111
- f) 0.0625_{10} = 00000001

Convert these fixed-point binary bytes to decimal where the first 3 bits represent the whole number part and the the last 5 bits represent the fractional part:

- g) 10101010_2 = 5.3125
- h) 10111011_2 = 5.84375
- i) 00111011_2 = 1.84375
- j) 11111000_2 = 7.75
- k) 00011111_2 = 0.96875
- l) 11111111_2 = 7.96875